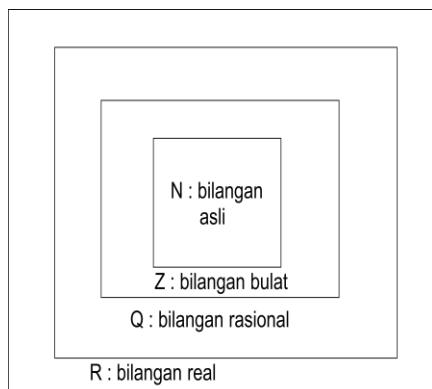


Pertemuan 1 SISTEM BILANGAN REAL

Sistem Bilangan



$$\mathbb{N} = \{1, 2, 3, 4, 5, \dots\}$$

$$\mathbb{Z} = \{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$$

$$\mathbb{Q} = \left\{ \frac{a}{b} \mid a, b \in \mathbb{Z}, b \neq 0 \right\}$$

Apakah $3,25$ $1,33\bar{3}$ $6,25\bar{2}\bar{5}$ $7,124\bar{2}\bar{4}$

Merupakan bilangan rasional?

Bagaimana dengan $\sqrt{2}$ $\sqrt{3}$ $3,1154672 \dots$ π

$$\mathbb{R} = \mathbb{Q} \cup \text{Irasional}$$

Contoh 1

Misalkan $x = 6,25\bar{2}\bar{5}$ maka $100x = 625,25\bar{2}\bar{5}$ sehingga

$$\begin{array}{r} 100x = 625,25\bar{2}\bar{5} \\ x = 6,25\bar{2}\bar{5} \\ \hline 99x = 619 \\ x = \frac{619}{99} \end{array}$$

Jadi x adalah bilangan rasional.

Contoh 2

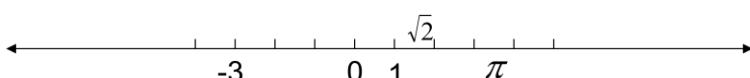
Misalkan $x = 7,124\bar{2}\bar{4}$ maka $1000x = 7124,24\bar{2}\bar{4}$ sehingga

$$\begin{array}{r} 1000x = 7124,24\bar{2}\bar{4} \\ 10x = 71,24\bar{2}\bar{4} \\ \hline 990x = 7053 \\ x = \frac{7053}{990} \end{array}$$

Jadi x adalah bilangan rasional.

Garis Bilangan Real

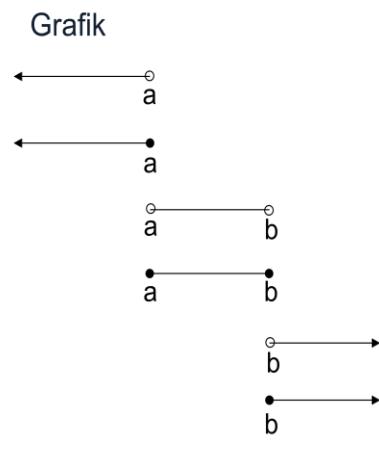
Setiap bilangan real mempunyai posisi pada suatu garis yang disebut dengan **garis bilangan (real)**.



Selang/Interval

Himpunan bagian dari garis bilangan

Himpunan	selang
$\{x x < a\}$	$(-\infty, a)$
$\{x x \leq a\}$	$(-\infty, a]$
$\{x a < x < b\}$	(a, b)
$\{x a \leq x \leq b\}$	$[a, b]$
$\{x x > b\}$	(b, ∞)
$\{x x \geq b\}$	$[b, \infty)$
$\{x x \in \mathbb{R}\}$	$(-\infty, \infty)$



Menyelesaikan Pertidaksamaan

Contoh 1

$$13 \geq 2x - 3 \geq 5$$

$$13 + 3 \geq 2x \geq 5 + 3$$

$$16 \geq 2x \geq 8$$

$$8 \geq x \geq 4$$

$$4 \leq x \leq 8$$

$$\text{Hp} = [4, 8]$$



Contoh 2

$$-2 < 6 - 4x \leq 8$$

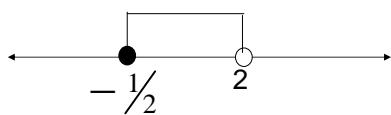
$$-8 < -4x \leq 2$$

$$\text{Hp} = \left[-\frac{1}{2}, 2 \right)$$

$$8 > 4x \geq -2$$

$$-2 \leq 4x < 8$$

$$-\frac{1}{2} \leq x < 2$$

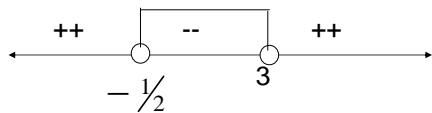


Contoh 3

$$2x^2 - 5x - 3 < 0$$

$$(2x+1)(x-3) < 0$$

Titik Pemecah (TP) : $x = -\frac{1}{2}$ dan $x = 3$



$$Hp = \left(-\frac{1}{2}, 3\right)$$

Contoh 4

$$2x - 4 \leq 6 - 7x \leq 3x + 6$$

$$2x - 4 \leq 6 - 7x \quad \text{dan} \quad 6 - 7x \leq 3x + 6$$

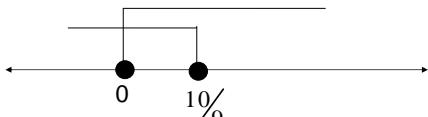
$$2x + 7x \leq 6 + 4 \quad \text{dan} \quad -7x - 3x \leq -6 + 6$$

$$9x \leq 10 \quad \text{dan} \quad -10x \leq 0$$

$$x \leq \frac{10}{9} \quad \text{dan} \quad 10x \geq 0$$

$$x \leq \frac{10}{9} \quad \text{dan} \quad x \geq 0$$

$$Hp = \left(-\infty, \frac{10}{9}\right] \cap [0, \infty)$$



Dari gambar tersebut dapat disimpulkan :

$$Hp = \left[0, \frac{10}{9}\right]$$

Contoh 5

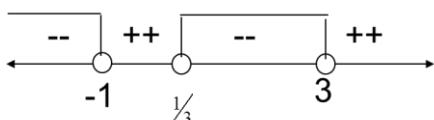
$$\frac{1}{x+1} < \frac{2}{3x-1}$$

$$\frac{1}{x+1} - \frac{2}{3x-1} < 0$$

$$\frac{(3x-1)-(2x+2)}{(x+1)(3x-1)} < 0$$

$$\frac{x-3}{(x+1)(3x-1)} < 0$$

$$TP : -1, \quad \frac{1}{3}, \quad 3$$



$$Hp = (-\infty, -1) \cup \left(\frac{1}{3}, 3\right)$$

Contoh 6

$$\frac{x+1}{2-x} \leq \frac{x}{3+x}$$

$$\frac{x+1}{2-x} - \frac{x}{3+x} \leq 0$$

$$\frac{(x+1)(3+x) - x(2-x)}{(2-x)(3+x)} \leq 0$$

$$\frac{2x^2 + 2x + 3}{(2-x)(x+3)} \leq 0$$

Untuk pembilang $2x^2 + 2x + 3$ mempunyai nilai

Diskriminan (D) < 0, sehingga nilainya selalu positif, Jadi TP : 2,-3

Pembilang tidak menghasilkan titik pemecah.



$$Hp = (\infty, -3) \cup (2, \infty)$$

Pertidaksamaan Nilai Mutlak

Nilai mutlak x ($|x|$) didefinisikan sebagai jarak x dari titik pusat pada garis bilangan, sehingga jarak selalu bernilai positif.

Definisi nilai mutlak

$$|x| = \begin{cases} x, & x \geq 0 \\ -x, & x < 0 \end{cases}$$

Sifat-sifat Nilai Mutlak

1. $|x| = \sqrt{x^2}$
2. $|x| \leq a$, dengan $a > 0$ jika dan hanya jika $-a \leq x \leq a$
3. $|x| \geq a$, dengan $a > 0$ jika dan hanya jika $x \geq a$ atau $x \leq -a$
4. $|x| \leq |y|$ jika dan hanya jika $x^2 \leq y^2$
5. $\left| \frac{x}{y} \right| = \frac{|x|}{|y|}$
6. $|x+y| \leq |x| + |y|$
7. $|x-y| \geq ||x|-|y||$

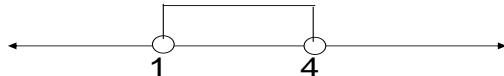
Contoh 1

$$|2x-5| < 3$$

Kita bisa menggunakan sifat ke-2.

$$\begin{aligned} &\Leftrightarrow -3 < 2x - 5 < 3 \\ &\Leftrightarrow 5 - 3 < 2x < 3 + 5 \\ &\Leftrightarrow 2 < 2x < 8 \\ &\Leftrightarrow 1 < x < 4 \end{aligned}$$

$$Hp = (1, 4)$$



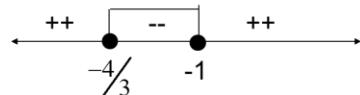
Contoh 2

$$|2x+3| \geq |4x+5|$$

Kita bisa menggunakan sifat 4

$$\begin{aligned} &\Leftrightarrow (2x+3)^2 \geq (4x+5)^2 \\ &\Leftrightarrow 4x^2 + 12x + 9 \geq 16x^2 + 40x + 25 \\ &\Leftrightarrow -12x^2 - 28x - 16 \geq 0 \\ &\Leftrightarrow 3x^2 + 7x + 4 \leq 0 \\ \text{TP: } & -\frac{4}{3}, -1 \end{aligned}$$

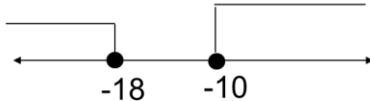
Jika digambar pada garis bilangan :



$$Hp = (-4/3, -1)$$

Contoh 3

$$\begin{aligned} &\left| \frac{x}{2} + 7 \right| \geq 2 \\ &\Leftrightarrow \frac{x}{2} + 7 \geq 2 \quad \text{atau} \quad \frac{x}{2} + 7 \leq -2 \\ &\Leftrightarrow \frac{x}{2} \geq -5 \quad \text{atau} \quad \frac{x}{2} \leq -9 \\ &\Leftrightarrow x \geq -10 \quad \text{atau} \quad x \leq -18 \\ &Hp = [-10, \infty) \cup (-\infty, -18] \end{aligned}$$



Latihan 1

Carilah himpunan penyelesaian dari:

1. $-8 \leq 5x - 3 < 12$
2. $14 > 2 - 3x \geq 3$
3. $3x^2 - 14x - 5 \geq 0$
4. $x + 5 \leq 5x - 3 < 2x + 12$
5. $\frac{2}{x+2} \geq \frac{1}{2x-1}$
6. $\left| \frac{x+2}{5} \right| < 3$
7. $|3x + 5| \geq 2$
8. $|2x - 3| \leq |2x + 12|$